

**6665**  
**Edexcel GCE**  
**Pure Mathematics C3**  
**Advanced Level**  
**Specimen Paper**

**Time: 1 hour 30 minutes**

**Materials required for examination**

Answer Book (AB16)  
Mathematical Formulae (Lilac)  
Graph Paper (ASG2)

**Items included with question papers**

Nil

**Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments TI-89, TI-92, Casio *cfx* 9970G, Hewlett Packard HP 48G.**

**Instructions to Candidates**

In the boxes on the answer book, write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Pure Mathematics C3), the paper reference (6665), your surname, other name and signature.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

**Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

This paper has seven questions.

**Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the Examiner. Answers without working may gain no credit.

1. The function  $f$  is defined by

$$f: x \mapsto |x - 2| - 3, x \in \mathbb{R}.$$

(a) Solve the equation  $f(x) = 1$ .

(3)

The function  $g$  is defined by

$$g: x \mapsto x^2 - 4x + 11, x \geq 0.$$

(b) Find the range of  $g$ .

(3)

(c) Find  $gf(-1)$ .

(2)

2.  $f(x) = x^3 - 2x - 5$ .

(a) Show that there is a root  $\alpha$  of  $f(x) = 0$  for  $x$  in the interval  $[2, 3]$ .

(2)

The root  $\alpha$  is to be estimated using the iterative formula

$$x_{n+1} = \sqrt{\left(2 + \frac{5}{x_n}\right)}, \quad x_0 = 2.$$

(b) Calculate the values of  $x_1, x_2, x_3$  and  $x_4$ , giving your answers to 4 significant figures.

(3)

(c) Prove that, to 5 significant figures,  $\alpha$  is 2.0946.

(3)

3. (a) Using the identity for  $\cos(A + B)$ , prove that  $\cos \theta \equiv 1 - 2 \sin^2\left(\frac{1}{2} \theta\right)$ .

(3)

(b) Prove that  $1 + \sin \theta - \cos \theta \equiv 2 \sin\left(\frac{1}{2} \theta\right) [\cos\left(\frac{1}{2} \theta\right) + \sin\left(\frac{1}{2} \theta\right)]$ .

(3)

(c) Hence, or otherwise, solve the equation

$$1 + \sin \theta - \cos \theta = 0, \quad 0 \leq \theta < 2\pi.$$

(4)

4. 
$$f(x) = x + \frac{3}{x-1} - \frac{12}{x^2+2x-3}, x \in \mathbb{R}, x > 1.$$

(a) Show that  $f(x) = \frac{x^2+3x+3}{x+3}$ . (5)

(b) Solve the equation  $f'(x) = \frac{22}{25}$ . (5)

5. **Figure 1**

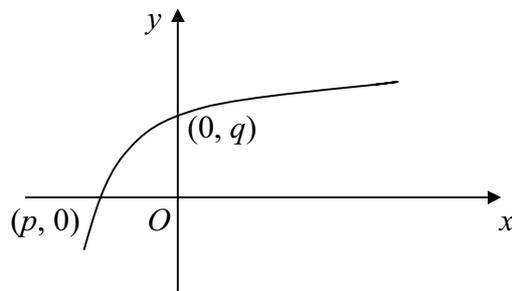


Figure 1 shows part of the curve with equation  $y = f(x)$ ,  $x \in \mathbb{R}$ . The curve meets the  $x$ -axis at  $P(p, 0)$  and meets the  $y$ -axis at  $Q(0, q)$ .

(a) On separate diagrams, sketch the curve with equation

(i)  $y = |f(x)|$ ,

(ii)  $y = 3f(\frac{1}{2}x)$ .

In each case show, in terms of  $p$  or  $q$ , the coordinates of points at which the curve meets the axes.

(5)

Given that  $f(x) = 3 \ln(2x + 3)$ ,

(b) state the exact value of  $q$ , (1)

(c) find the value of  $p$ , (2)

(d) find an equation for the tangent to the curve at  $P$ . (4)

6. As a substance cools its temperature,  $T$  °C, is related to the time ( $t$  minutes) for which it has been cooling. The relationship is given by the equation

$$T = 20 + 60e^{-0.1t}, \quad t \geq 0.$$

- (a) Find the value of  $T$  when the substance started to cool. (1)
- (b) Explain why the temperature of the substance is always above 20°C. (1)
- (c) Sketch the graph of  $T$  against  $t$ . (2)
- (d) Find the value, to 2 significant figures, of  $t$  at the instant  $T = 60$ . (4)
- (e) Find  $\frac{dT}{dt}$ . (2)
- (f) Hence find the value of  $T$  at which the temperature is decreasing at a rate of 1.8 °C per minute. (3)
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7. (i) Given that  $y = \tan x + 2 \cos x$ , find the exact value of  $\frac{dy}{dx}$  at  $x = \frac{\pi}{4}$ . (3)
- (ii) Given that  $x = \tan \frac{1}{2}y$ , prove that  $\frac{dy}{dx} = \frac{2}{1+x^2}$ . (4)
- (iii) Given that  $y = e^{-x} \sin 2x$ , show that  $\frac{dy}{dx}$  can be expressed in the form  $R e^{-x} \cos (2x + \alpha)$ . Find, to 3 significant figures, the values of  $R$  and  $\alpha$ , where  $0 < \alpha < \frac{\pi}{2}$ . (7)
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**END**